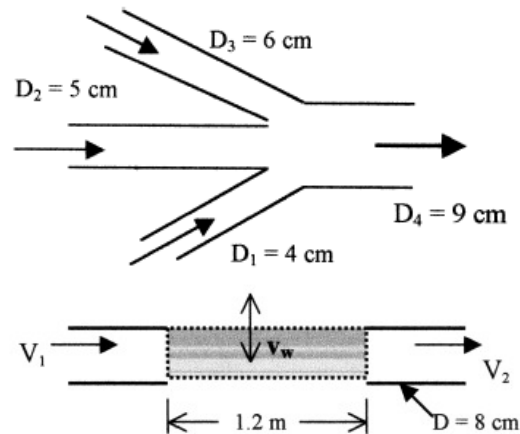


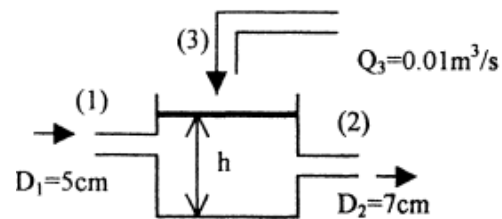
CE 371 HOMEWORK 6

1) Three pipes steadily deliver water at 20°C to a large exit pipe as shown in the figure. The velocity $V_2 = 5$ m/s, and the exit flow rate $Q_4 = 120$ m³/h. Find (a) V_1 ; (b) V_3 ; and (c) V_4 if it is known that increasing Q_3 by 20% would increase Q_4 by 10%



2) Water flowing through an 8-cm-diameter pipe enters a porous section, as shown in the figure, which allows a uniform radial velocity v_w through the wall surfaces for a distance of 1.2 m. If the entrance average velocity V_1 is 12 m/s, find the exit velocity V_2 if (a) $v_w = 15$ cm/s out of the pipe walls; (b) $v_w = 10$ cm/s into the pipe. (c) What value of v_w will make $V_2 = 9$ m/s?

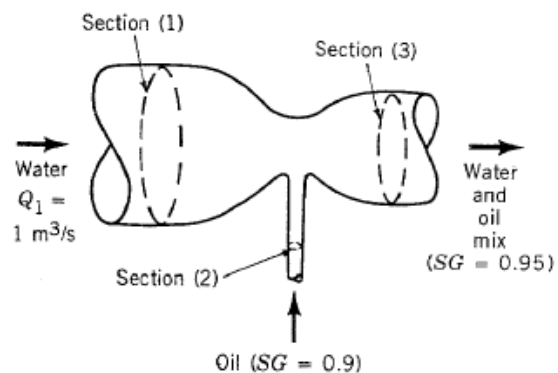
3) The open tank in the figure contains Water. If h is constant, determine V_2 for the given data if $V_1 = 3$ m/s and $Q_3 = 0.01$ m³/s.



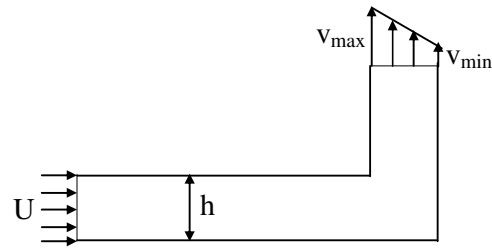
4) Viscous liquid from a circular tank, $D = 300$ mm in diameter, drains through a long circular tube of radius $R = 50$ mm. The velocity profile at the tube discharge is

$$u = u_{\max} \left[1 - \left(\frac{r}{R} \right)^2 \right]. \text{ Show that the average speed of flow in the drain tube is } V_{\text{ave}} = \frac{1}{2} u_{\max}.$$

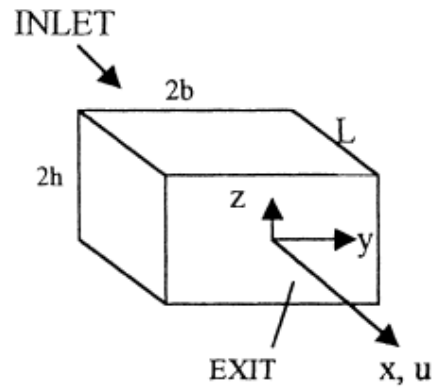
5) Oil having a specific gravity 0.9 is pumped as illustrated in the figure with a water jet pump. The water volume flowrate is 1 m³/s. The water and oil mixture has an average specific gravity of 0.95. Calculate the rate, in m³/s, at which the pump moves oil.



6) Water enters a two dimensional square channel of constant width $h = 75.5 \text{ mm}$, with uniform velocity U . The channel makes a 90° bend that distorts the flow to produce the linear velocity profile as shown at the exit, with $v_{\max} = 2v_{\min}$. Evaluate the $v_{\min}$, if $U = 7.5 \text{ m/s}$.



7) An incompressible fluid flows steadily through the rectangular duct in the figure. The exit velocity profile is given by $u = u_{\max}(1 - y^2/b^2)(1 - z^2/h^2)$. (a) Does this profile satisfy the correct boundary conditions for viscous fluid flow? (b) Find an analytical expression for the volume flow Q at the exit. (c) If the inlet flow is $0.1416 \text{ m}^3/\text{s}$, estimate $u_{\max}$ in m/s . ($b = h = 10 \text{ cm}$)



ANSWERS

1) a) $V_1 = 5.45 \text{ m/s}$; b) $V_3 = 5.89 \text{ m/s}$; c) $V_4 = 5.24 \text{ m/s}$

2) a) $V_2 = 3 \text{ m/s}$; b) $V_2 = 18 \text{ m/s}$; c) $v_w = 0.05 \text{ m/s}$ (out).

3) a) $\frac{dh}{dt} = \frac{Q_1 + Q_3 - Q_2}{(\pi d^2/4)}$; b) $V_2 = 4.13 \text{ m/s}$

5) $Q_2 = 1 \text{ m}^3/\text{s}$

6) $v_{\min} = 5.0 \text{ m/s}$

7) a) Yes; b) $Q = \frac{16bhu_{\max}}{9}$ c) $u_{\max} = 7.96 \text{ m/s}$

CE 371 HOMEWORK 6.2

Q1) For steady viscous flow through a circular tube, the

axial velocity profile is given by $u = U_0(1 - \frac{r}{R})^m$

as shown in the figure. For laminar flow $m \approx 1/2$ while for turbulent flow $m \approx 1/7$. (a) Compute the average velocity if the density is constant (b) Suppose the density also varies according to the formula

$$\rho = \frac{1}{2} \rho_0 \left[1 + \left(1 - \frac{r}{R} \right)^n \right] \quad \text{i.e. It increases from}$$

$0.5\rho_0$ at the walls to ρ_0 at the centreline. This simulates high speed gas flow through a tube with hot walls. Compute the average density and the average product of density and velocity, and compare. (For laminar flow $n \approx 1/2$ and for turbulent flow $n \approx 1/7$)

a) Laminar $\rightarrow V_{av} \approx 0.53 U_0$; Turbulent $\rightarrow V_{av} \approx 0.82 U_0$

b) Laminar $\rightarrow S_{av} \approx 0.77 S_0$; Turbulent $\rightarrow S_{av} \approx 0.91 S_0$

c) $(Sv)_{av} \approx 1.06 S_{av} V_{av}$ (laminar); $(Sv)_{av} \approx 1.01 S_{av} V_{av}$ (Turbulent)

Q2) Consider a device used to mix and deliver two liquids with roughly the same density 1050 kg/m^3 , as shown in the figure. For the conditions shown in the figure, find the maximum velocity after the two liquid streams mix. (u_{03} = maximum velocity)

The flow is assumed to be steady and incompressible.

$$u_{03} = 0.01 \text{ m/s}$$

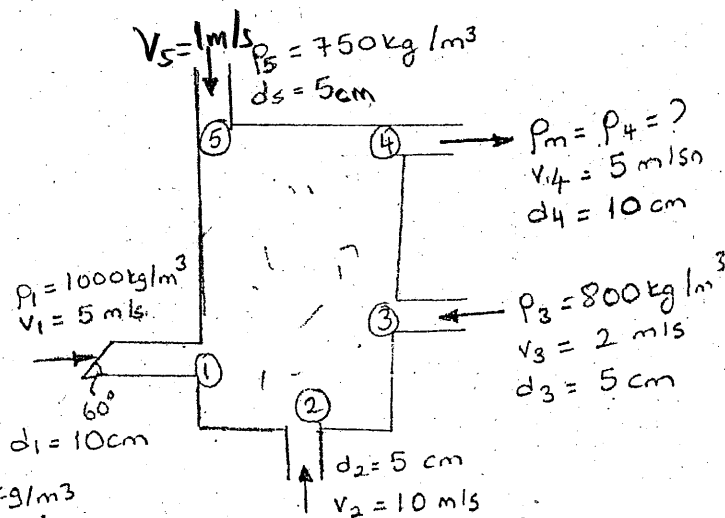
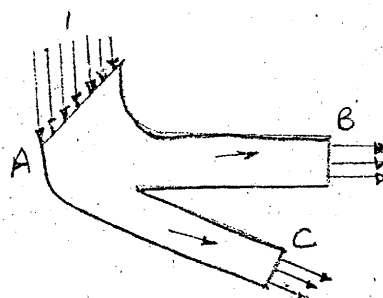
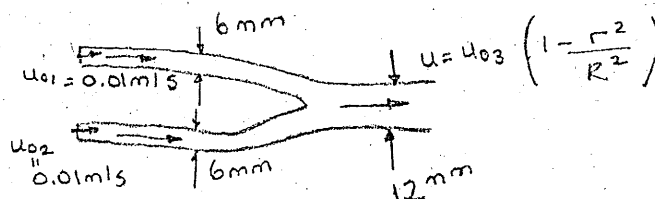
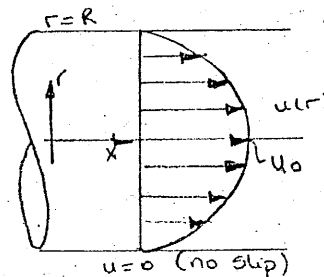
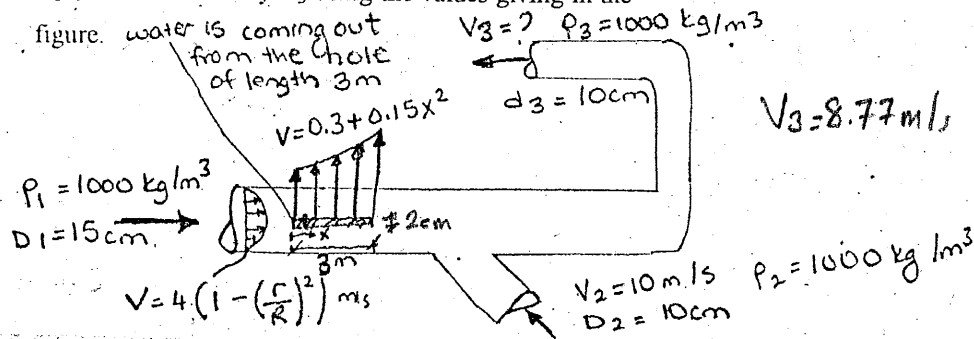
Q3) A two-dimensional water flow divider is shown in the figure. The flow in through opening A varies linearly from 3 m/s to 6 m/s and is inclined with an angle $\alpha = 45^\circ$ to the opening itself. The area of the A opening is $0.4 \text{ m}^2/\text{m}$, that of B is $0.2 \text{ m}^2/\text{m}$ and that of C is $0.15 \text{ m}^2/\text{m}$. The flow at B, normal to the opening, varies linearly from 3 m/s to 5 m/s, and the flow at C, normal to the opening, is approximately constant. Find q_c . Note that the flow is incompressible.

$$q_c = 3.153 \text{ m}^3/\text{s}$$

Q4) Assuming that the flow is incompressible and steady, find the density of the mixture ρ_m coming out of the tank using the values shown in the figure.

$$\rho_m = 1118 \text{ kg/m}^3$$

Q5) Find the velocity V_3 using the values giving in the figure. water is coming out from the hole of length 3m



CE 371 HOMEWORK 6.3

Q1) Consider an initially empty reservoir with volume 2 m³ connected to a supply line through a valve as shown in the figure. Find the time it takes to fully fill the reservoir when the valve opens.

$$(t_{fill} = 636.6 \text{ seconds})$$

$V_f(t)$ = volume of the tank at time t .

The flow at the supply line is assumed to be constant and incompressible.

Q2) For steady viscous flow through a circular tube, the

axial velocity profile is given by $u = U_0(1 - \frac{r^2}{R^2})^m$

as shown in the figure. For laminar flow $m \approx 1/2$ while for turbulent flow $m \approx 1/7$. (a) Compute the average velocity if the density is constant (b) Suppose the density also varies, according to the formula

$$\rho = \frac{1}{2} \rho_0 \left[1 + \left(1 - \frac{r}{R} \right)^n \right] \text{ i.e. It increases from}$$

$0.5\rho_0$ at the walls to ρ_0 at the centreline. This simulates high speed gas flow through a tube with hot walls. Compute the average density and the average product of density and velocity, and compare. (For laminar flow $n \approx 1/2$ and for turbulent flow $n \approx 1/7$)

$$V_{av} \approx 0.53 u_0 (\text{lamin.}) \quad \bar{\rho}_{av} = 0.77 \rho_0 (\text{lamin.})$$

$$V_{av} \approx 0.82 u_0 (\text{turb.}) \quad \bar{\rho}_{av} = 0.91 \rho_0 (\text{turb.})$$

Q3) Consider a device used to mix and deliver two liquids with roughly the same density 1050 kg/m³, as shown in the figure. For the conditions shown in the figure, find the maximum velocity after the two liquid streams mix. (u_{03} = maximum velocity)

The flow is assumed to be steady and incompressible. $u_{03} = 0.01 \text{ m/s}$

Q4) The tank given in the figure is being filled with water by two one-dimensional inlets. Air is trapped at the top of the tank. The water height is h . (a) Find an expression for the change in water height dh/dt . (b) Compute dh/dt if $D_1 = 2.5 \text{ cm}$, $D_2 = 7.6 \text{ cm}$, $V_1 = 0.91 \text{ m/s}$, $V_2 = 0.61 \text{ m/s}$ and $A_t = 0.186 \text{ m}^2$, assuming water at 20°C

$$a) \frac{dh}{dt} = \frac{Q_1 + Q_2}{A_t} \quad b) 0.0173 \text{ m/s}$$

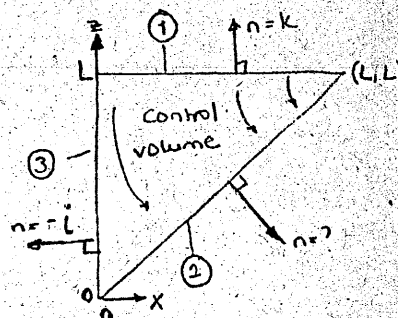
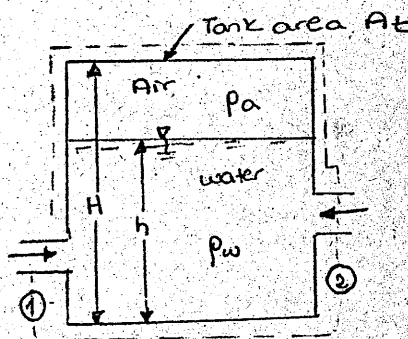
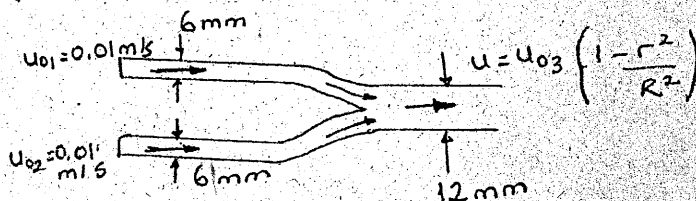
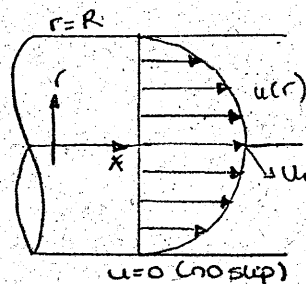
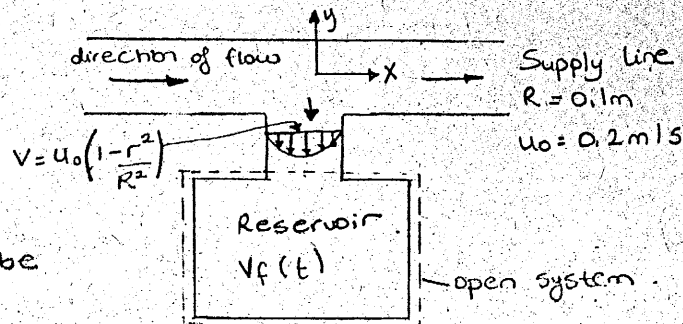
Q5) Consider the constant-density velocity field

$$u = \frac{V_0 x}{L}, \quad v = 0 \quad \text{and} \quad w = -\frac{V_0 z}{L} \text{ Use the}$$

triangular control volume given in the figure, bounded by (0, 0), (L, L) and (0, L), with depth b into paper. Compute the volume flow through sections 1, 2 and 3 and compare to see whether mass is conserved.

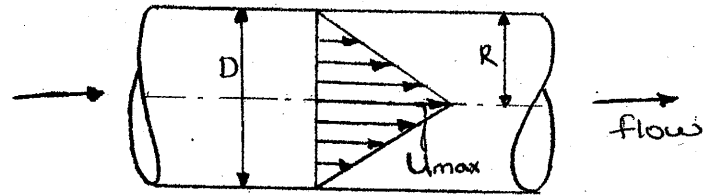
$$Q_1 = -V_0 b L \quad Q_2 = V_0 b L$$

$$Q_3 = 0$$



depth b into paper

Q1) Water flowing out of a circular pipe is assumed to have a linearly varying velocity distribution as shown in the figure. What is the average velocity of the outward flow in terms of U_{max} . ($\frac{U_{max}}{3} = V_{ave}$)

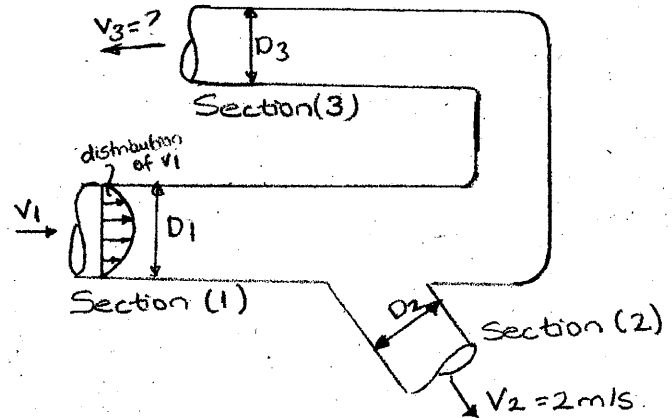


Q2) Water flows into a branched pipe as shown in the figure. The diameters of the pipes are $D_1=20\text{cm}$, $D_2=10\text{cm}$ and $D_3=5\text{cm}$. The velocity profile of the water entering the pipe is given by

$$V_1 = 0.25 \left[1 - \frac{r^2}{R_1^2} \right] \text{ where } R_1 \text{ is the radius of the pipe}$$

at Section 1. If the uniform velocity at Section 2 is $V_2=2\text{ m/s}$, then find the average velocity at Section 3.

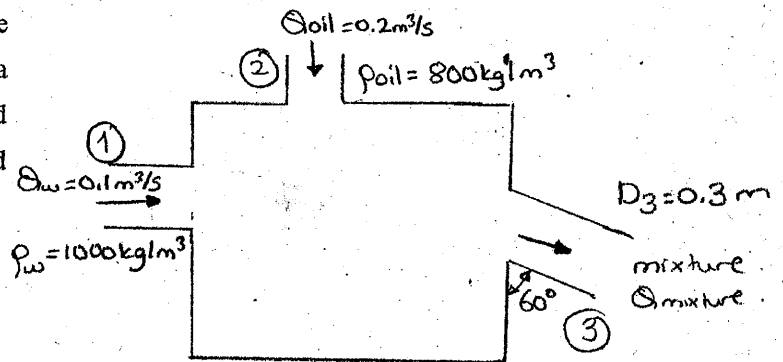
$$V_3 = 6.01 \text{ m/s (inward)}$$



Q3) Oil and water are mixing in the tank and the mixture is flowing out from the pipe which has a diameter of 0.3m . If the discharge of oil is $0.2\text{ m}^3/\text{s}$ and the discharge of water is $0.1\text{ m}^3/\text{s}$, find the velocity and the density of the mixture.

$$V_{mix} = 4.244 \text{ m/s}$$

$$\rho_{mix} = 866.67 \text{ kg/m}^3$$



Q4) Consider the constant-density velocity field

$$u = \frac{V_0 x}{L}, \quad v = 0 \quad \text{and} \quad w = -\frac{V_0 z}{L}$$

Use the triangular control volume given in the figure, bounded by $(0, 0)$, (L, L) and $(0, L)$, with depth b into paper. Compute the volume flow through sections 1, 2 and 3 and compare to see whether mass is conserved.

$$Q_1 = -V_0 b L$$

$$Q_3 = 0$$

$$Q_2 = V_0 b L$$

Q5) Find the velocity V_3 using the values giving in the figure. ($V_3 = 1.47 \text{ m/s}$)

Velocity distribution at section 1 is given by

$$V_1 = 2 \left(1 - \frac{r^2}{R_1^2} \right)$$

Uniform velocity is present at Section 2 and Section 3

